

# Generation of Twisted Gamma-Rays Using Accelerated Ions

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In collaboration with

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Ann. Phys. (Berlin) 2022, 2200168. arXiv:2203.06988

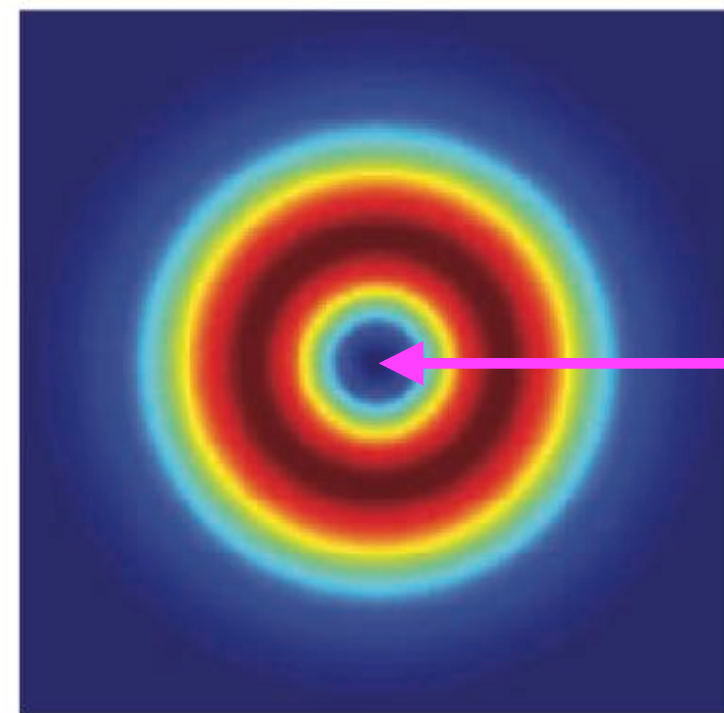
MMQS2022, Mie University, 2022/12/8

# Twisted photon(捩光子), optical vortex(光渦)

Orbital angular momentum (OAM) of light

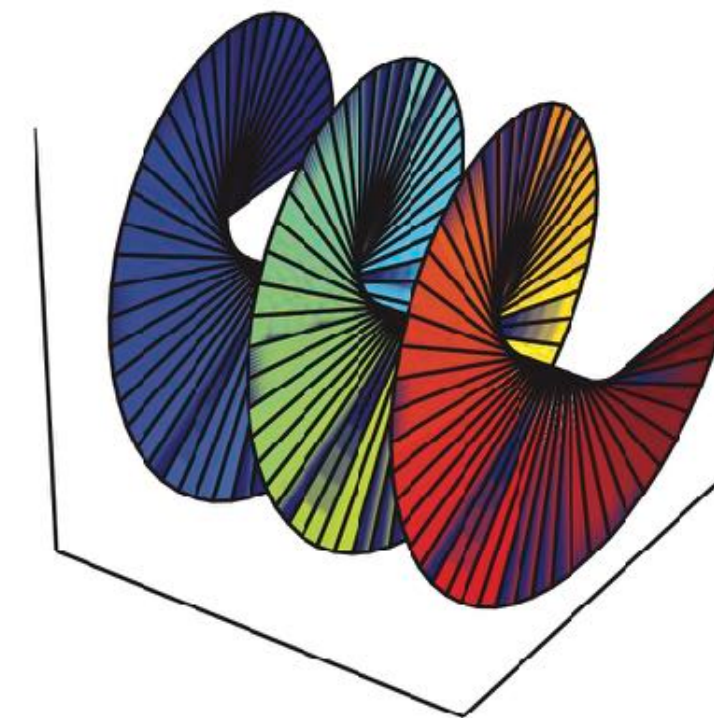
winding field phase  $\sim e^{im\varphi}$

G. Molina-Terriza et al.  
Nat. Phys. 3, 305 (2007)



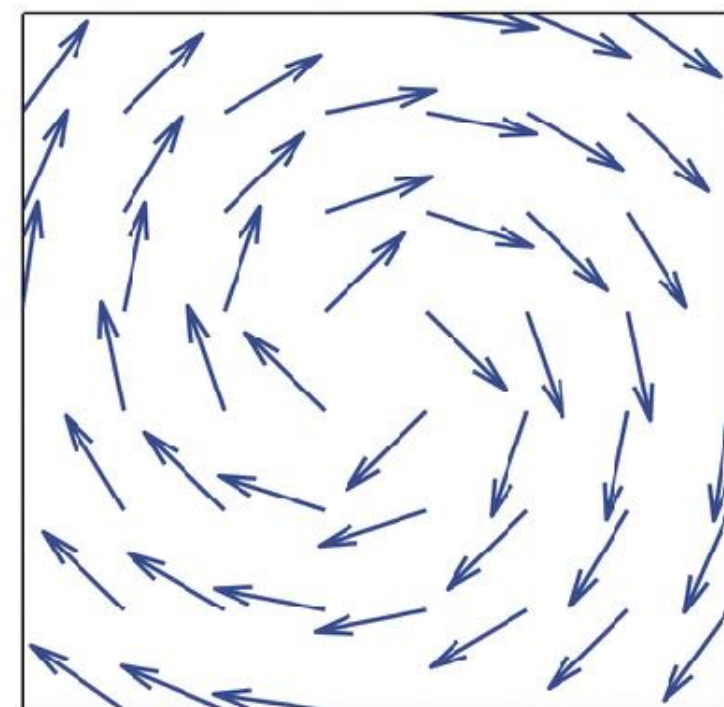
field intensity

phase  
singularity

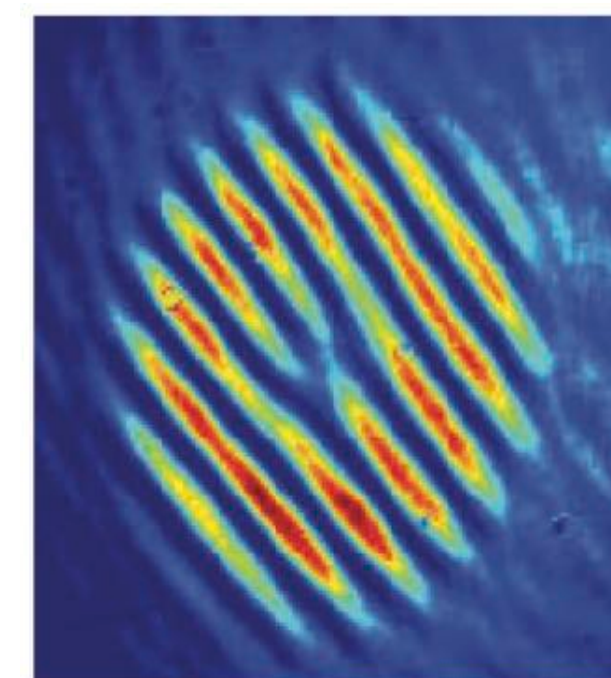


wave front

helicoid



transvers  
Poynting vector



Interference pattern  
with plane wave

computer-generated hologram

# Generation (and use) of twisted photons

## Optical region

Y. Shen et al., Light: Sci. & App. 8, 90 (2019)

fork hologram, lens-based mode converter, etc.

(micro manipulation, imaging, data transmission, etc.)

## X-ray region

helical undulator, FEL

S. Sasaki, I. McNulty, PRL 100, 124801 (2008)

E. Hemsing et al. Nat. Phys. 9, 549 (2013)

## Gamma-ray region (proposals)

backward Compton scattering

$$e + \gamma_{tw} \rightarrow e + \gamma_{tw}$$

U.D. Jentschura, V.G. Serbo, PRL 106, 013001 (2011)

nonlinear Thomson scattering

$$e + \gamma_{pw/tw} + \gamma_{pw/tw} + \dots \rightarrow e + \gamma_{tw} + \dots$$

Y. Taira, T. Hayakawa, M. Katoh, Sci. Rep. 7, 5018 (2017)

Y.-Y. Chen et al., Phys. Rev. Lett. 121, 074801 (2018)

Y.-Y. Liu et al., Opt. Lett. 48, 395 (2020)



# Gamma factory

E.G.Bessonov, NIMB 309, 92 (2013)

M.W. Krasny, CERN-SPSC-2019-031; SPSC-I-253

## Rayleigh scattering by boosted ion

$$\gamma_i + |g\rangle \rightarrow |e\rangle \rightarrow |g\rangle + \gamma_f$$

Lorentz boost  $E = \gamma M$

e.g.  $\gamma \sim 10^3$  @LHC

Level splitting:  $E_{eg}$

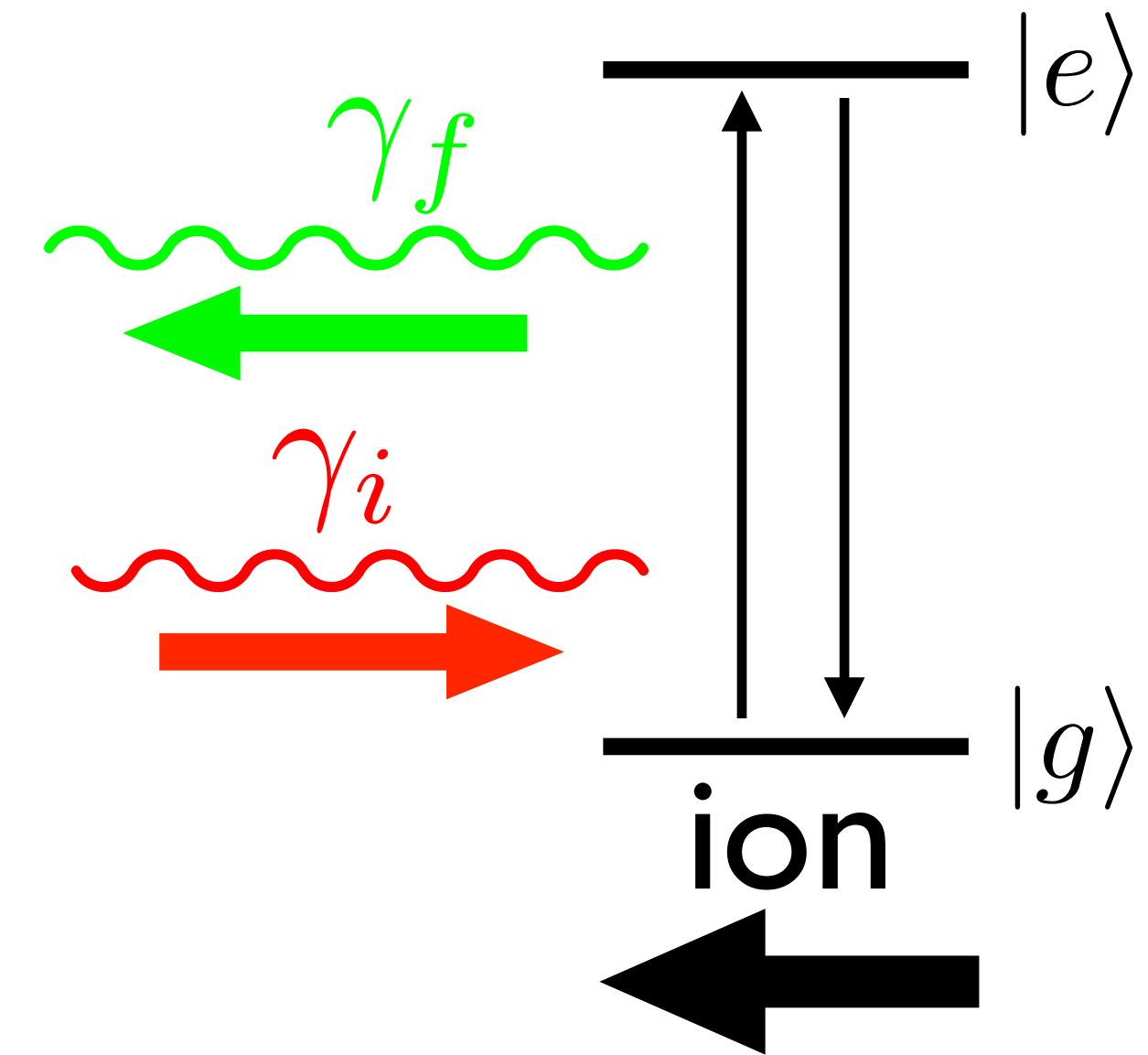
binding energy of H-like ion =  $(Z^2/n^2)13.6$  eV

Resonance condition:  $2\gamma\omega_i \simeq E_{eg}$   $\omega_i \sim 1-10$  eV

$\rightarrow Z^2/2\gamma \sim 0.1-1$

Up-conversion:

$$\omega_f^{\max} \simeq 2\gamma E_{eg} \simeq 4\gamma^2 \omega_i \sim 0.1-1 \text{ GeV} (2\gamma/10^4)^2$$



heavy ion

# Twisted photon generation by $2\gamma$ excitation

Excitation to a state of large angular momentum

$$2\gamma \text{ absorption } \gamma_{\text{pw}} + \gamma_{\text{pw}} + I \rightarrow I^*$$

$$\text{Raman process } \gamma_{\text{pw}} + I \rightarrow I^* + \gamma_{\text{pw}}$$

Efficient population transfer

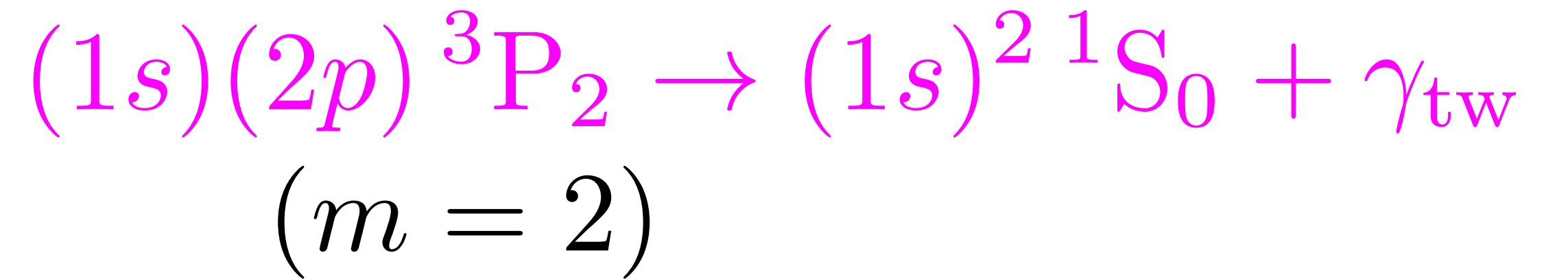
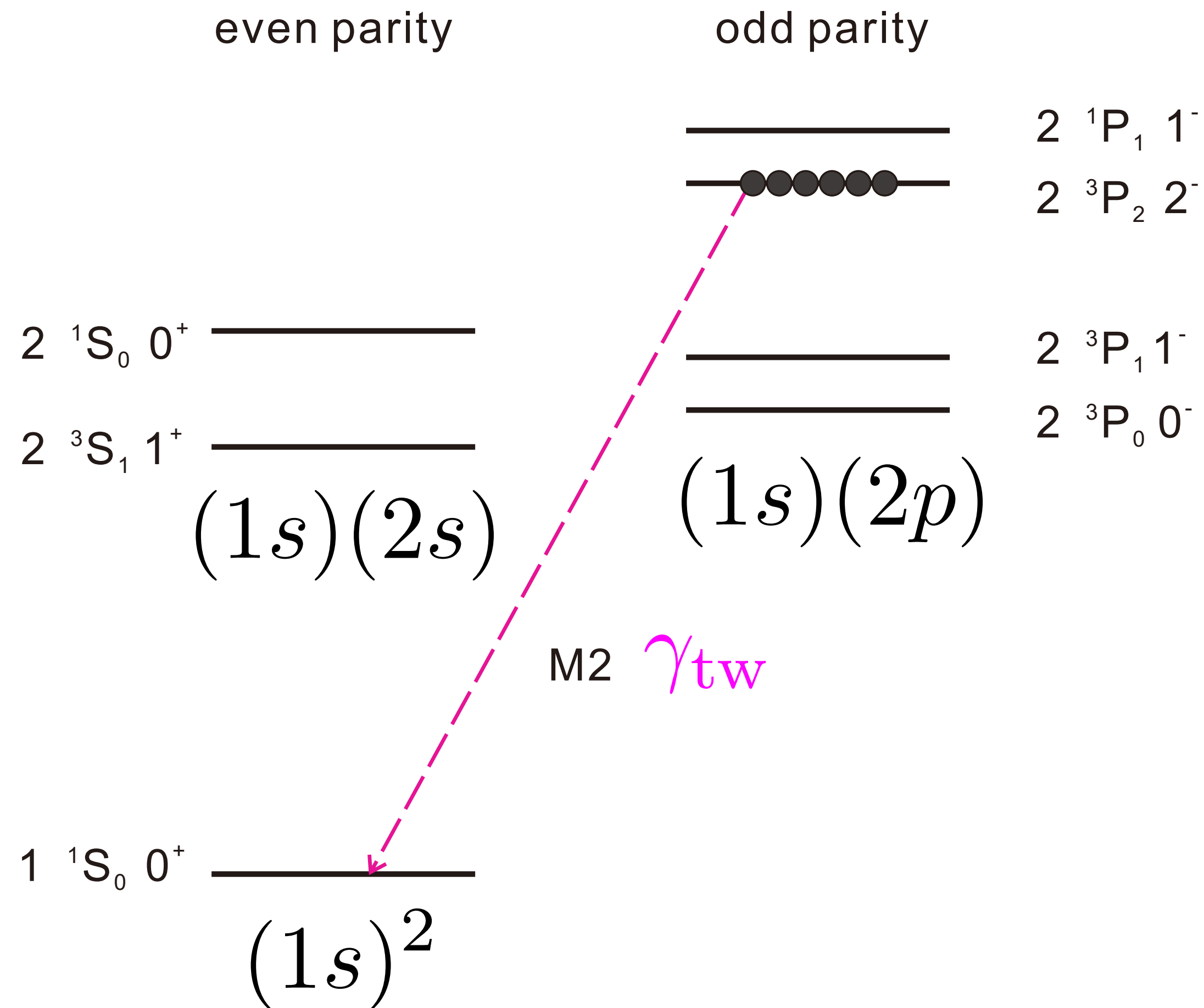
by Stimulated Raman Adiabatic Passage (**STIRAP**)

Twisted photon generation in de-excitation

$$I^* \rightarrow I + \gamma_{\text{tw}}$$

He-like ions considered

# Twisted photons from He-like ions

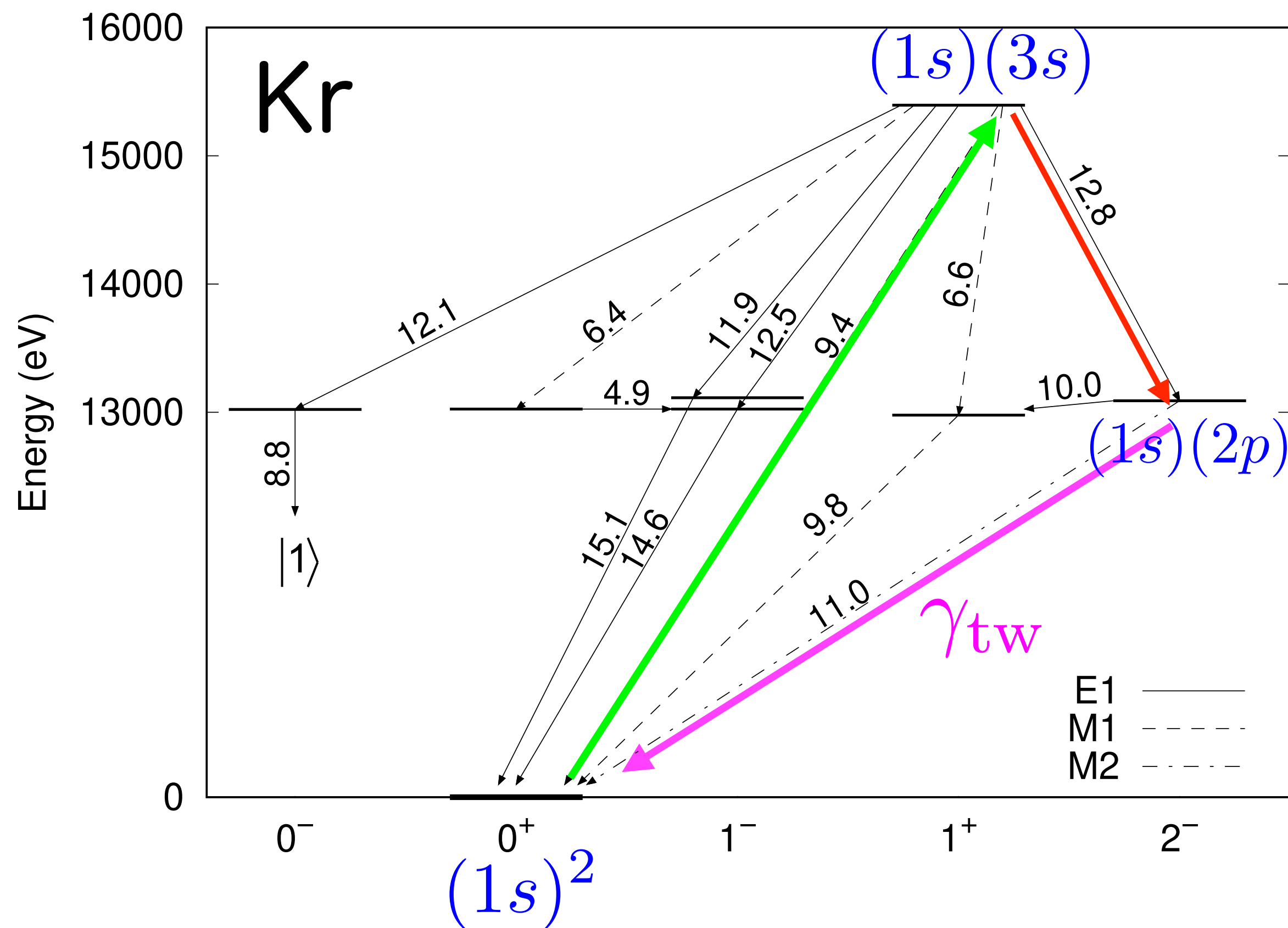


M2 transition dominates.  
 $\propto Z^8$  heavy ions

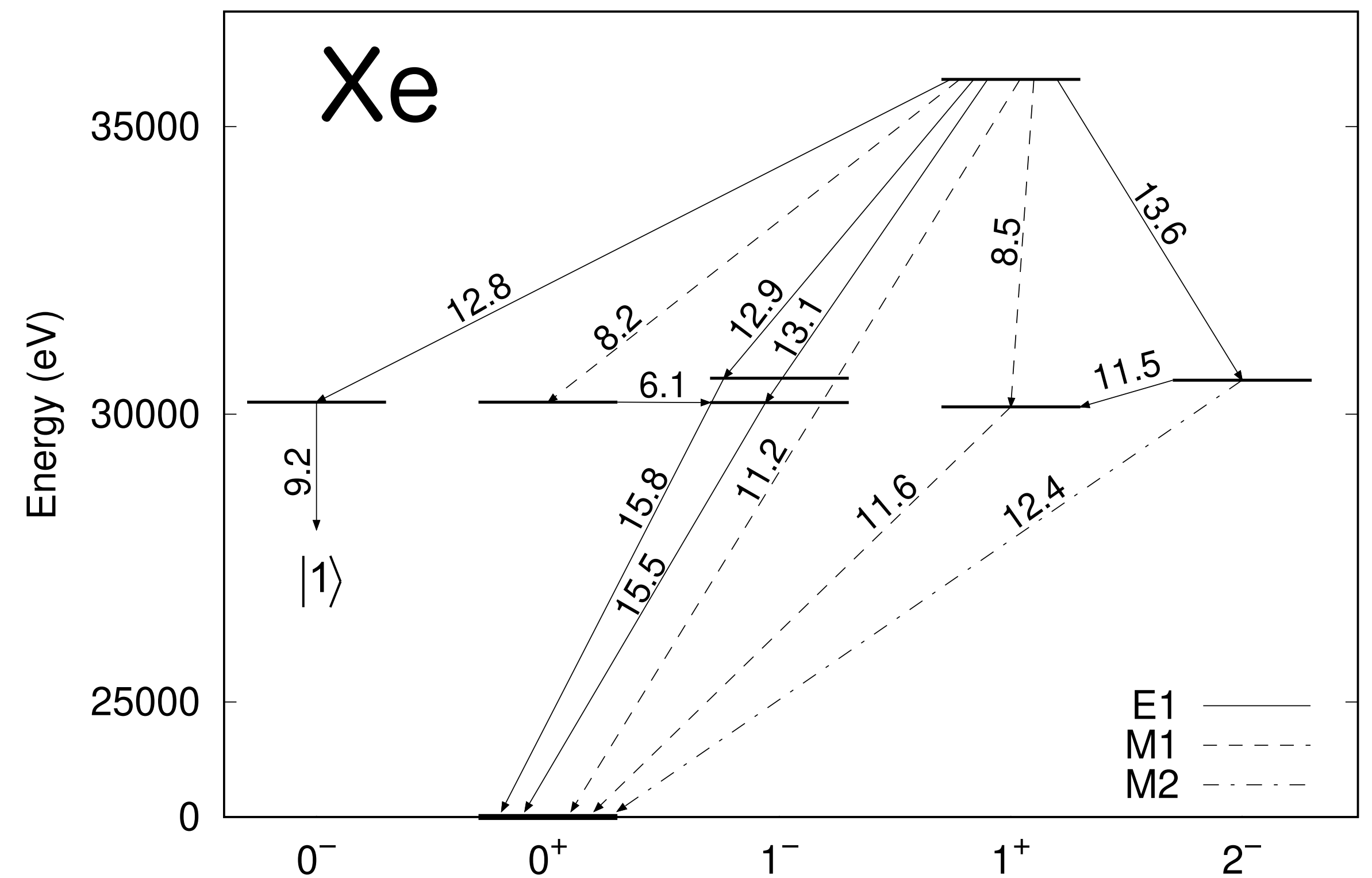
Kr ( $Z=36$ ), Xe ( $Z=54$ ) studied

# Levels and transitions of He-like ions

Calculation by GRASP2018 (MCDHF+RCI)

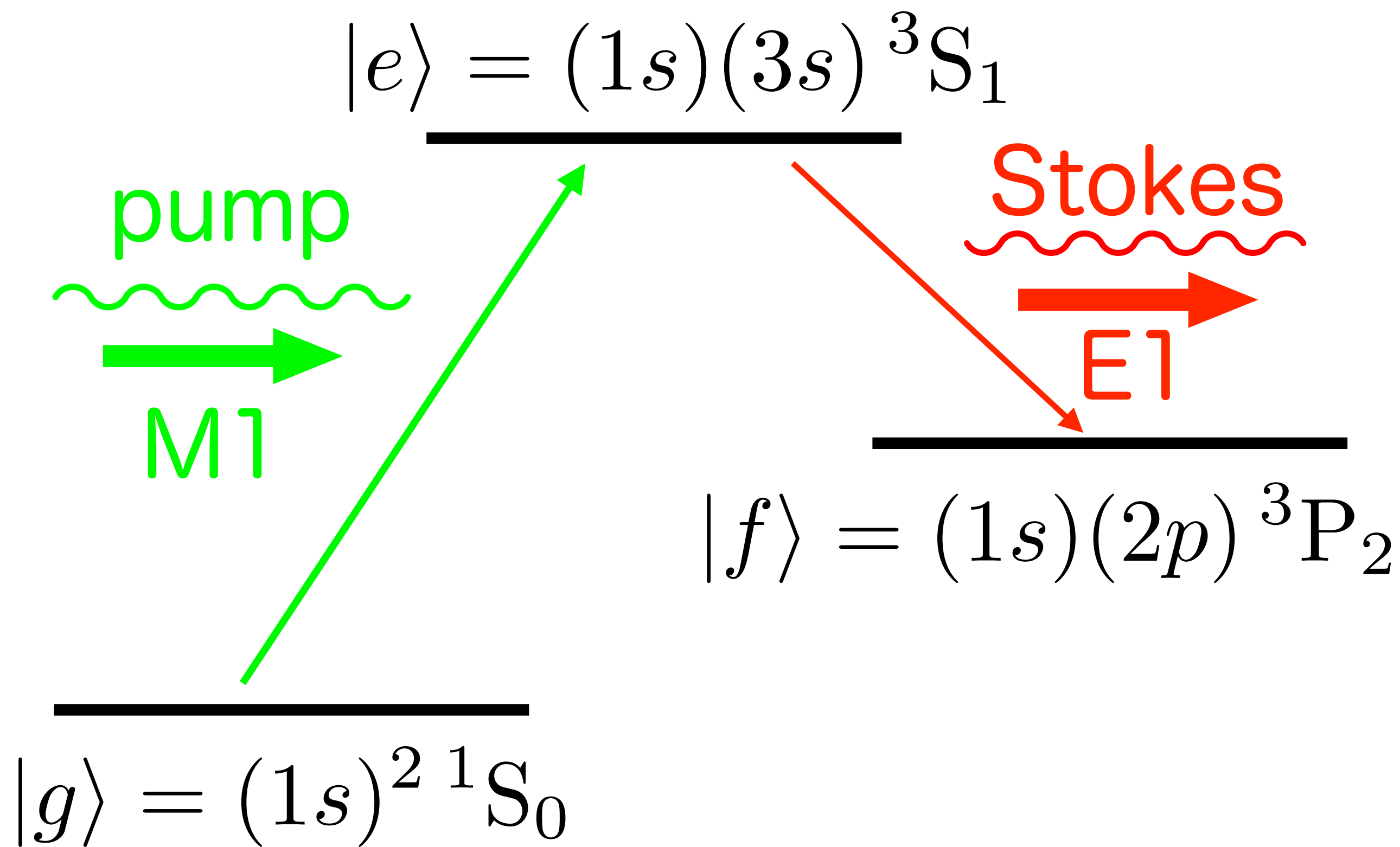


$$E_{\gamma_{tw}} = 65.4 \text{ MeV} \quad (\gamma_{ion} = 2500)$$



$$E_{\gamma_{tw}} = 306 \text{ MeV} \quad (\gamma_{ion} = 5000)$$

# Excitation scheme by STIRAP



Rabi freq. for 1W/mm<sup>2</sup>

Transitions	Type	Kr [s <sup>-1</sup> ]	Xe [s <sup>-1</sup> ]
$\Omega_p$ $ g\rangle \rightarrow  e\rangle$	M1	$5.570 \times 10^4$	$1.276 \times 10^5$
$\Omega_s$ $ e\rangle \rightarrow  f\rangle$	E1	$3.935 \times 10^7$	$2.882 \times 10^7$

pulse profile

Kr

pump, Stokes: opposite circular pol.



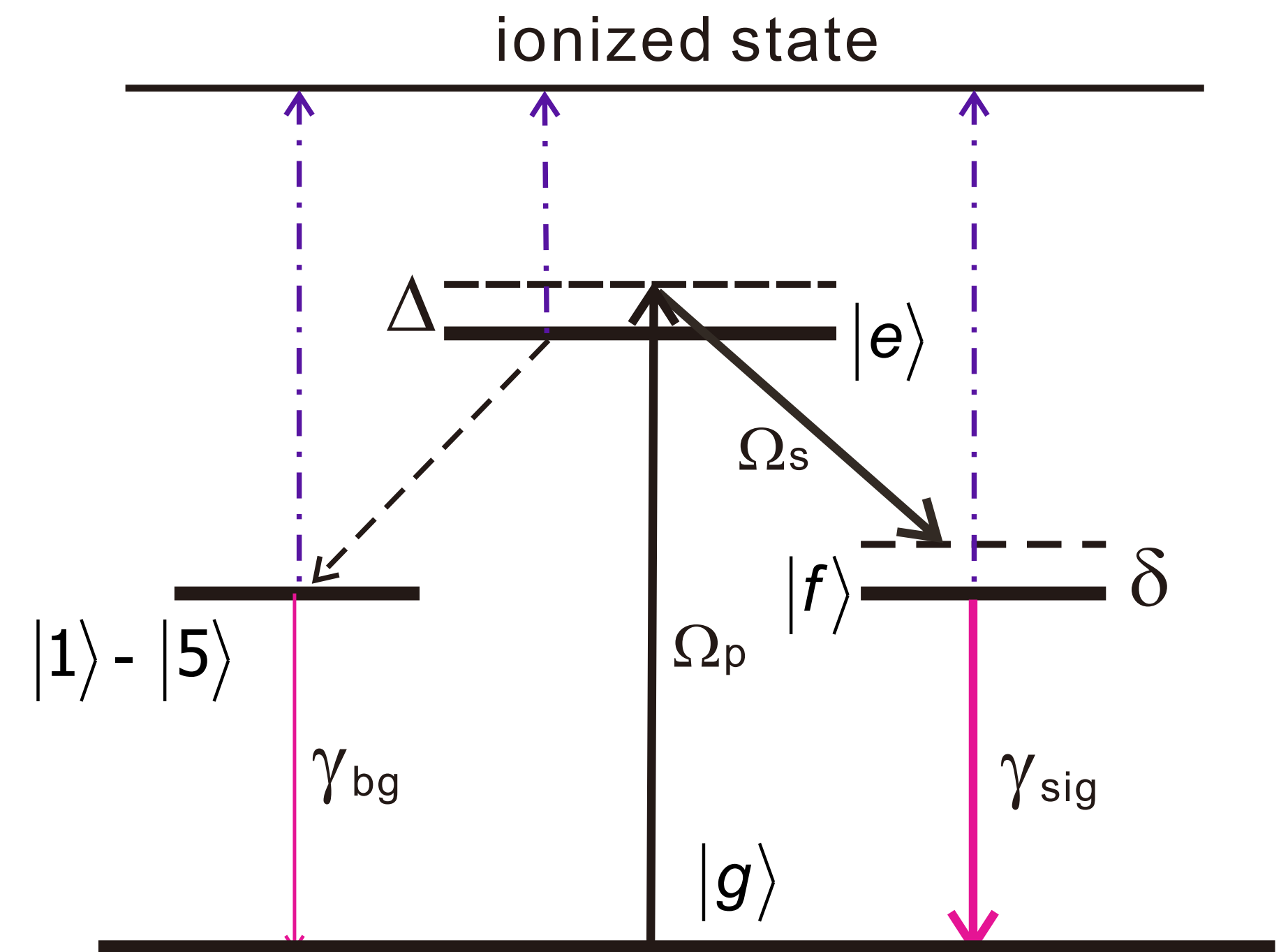
# Outline of numerical calculation

## Optical Bloch Equation

$$|g\rangle = (1s)^2 \ ^1S_0, |e\rangle = (1s)(3s) \ ^3S_1, |f\rangle = (1s)(2p) \ ^3P_2$$

and all other (1s)(2s) and (1s)(2p) states involved  
photo-ionization included

Parameter	Symbol	Kr	Xe	units
Lorentz boost factor	$\gamma_{ion}$	2500	5000	-
Pump laser wavelength	$\lambda_p$	403	346	nm
Pump laser intensity	$I_p(0)$	$4 \times 10^5$	$4 \times 10^5$	W/mm <sup>2</sup>
Stokes laser wavelength	$\lambda_s$	2690	2371	nm
Stokes laser intensity	$I_s(0)$	$4 \times 10^5$	$4 \times 10^5$	W/mm <sup>2</sup>
Laser pulse width	$\sigma_L$	1.0	1.0	nsec
Laser pulse delay	$t_d$	0.5	0.5	nsec
Pump laser detuning	$\Delta$	5	5	$\Gamma_e^{(tot)}$
Two-photon detuning	$\delta$	0	0	$\Gamma_e^{(tot)}$



# Results (Kr)

## Population

Kr

$|f\rangle$

$|e\rangle$

$$|1\rangle = (1s)(2s) {}^3S_1$$

# Signal, background, photo-ionization

Kr BG photons:  
from other 2s, 2p to 1s

$B/S=5.6\%$

Ion beam lifetime due to  
photo-ionization  $\sim 10^5$  sec.  
(A ring of 30 km  
circumference assumed)

# Results (Xe)

## Population

Xe



# Signal, background, photo-ionization

Xe

BG photons:  
from other 2s, 2p to 1s

$B/S=19.2\%$

Ion beam lifetime due to  
photo-ionization  $\sim 10^5$  sec.  
(A ring of 30 km  
circumference assumed)

# Summary

- Twisted gamma-ray from accelerated He-like ion  
**STIRAP**  $(1s)^2\ ^1S_0 \rightarrow (1s)(2p)\ ^3P_2$ , **M2** de-excitation
- Signal **65.4(306) MeV** for Kr(Xe) of boost 2500(5000)  
 $10^9$  ions/bunch  $\rightarrow$  **2.3(5.8)  $\times 10^8$  Hz/bunch**  $C_{\text{ring}} = 30$  km
- BG and ionization loss  
 **$B/S = 5.6(19.2)\%$** , loss fraction =  **$6.9(11) \times 10^{-10}$**
- Prospects  
Physics applications: nuclear, astro, plasma etc.  
Comparison with electron beam